



## 复旦大学数学科学学院 数学综合报告会

报告题目: On a problem of Fritz, Netzer, and Thom

报告人: Isaac Goldbring (加州大学尔湾分校)

时间: 2026-03-30 星期一 16:00 - 17:30

地点: 光华楼西主楼2401

报告摘要:

After being open for 50 years, the Connes Embedding Problem (CEP) in operator algebras was settled several years ago as a consequence of the quantum complexity result  $MIP^* = RE$ . One equivalent formulation of the CEP is that the group  $F_2 \times F_2$  is residually finite-dimensional (RFD), where  $F_2$  is the free group on 2 generators. In their 2012 paper, Fritz, Netzer, and Thom proved that any RFD group  $G$  is such that the standard presentation of the universal group  $C^*$ -algebra  $C^*(G)$  is computable and thus raised the question as to whether or not the standard presentation of the universal group  $C^*$ -algebra  $C^*(F_2 \times F_2)$  is computable, for a negative answer to this question would refute the CEP. While  $MIP^* = RE$  settled the CEP, it failed to resolve the question of Fritz, Netzer, and Thom. In this talk, I will show that the standard presentation of the universal group  $C^*$ -algebra  $C^*(F_2 \times F_2)$  is not computable, using an even more recent quantum complexity result known as  $MIP_{co} = coRE$ . Time permitting, I will discuss related results. The work presented in this talk is joint with Thomas Sinclair. No prior knowledge of operator algebras or quantum complexity will be assumed.

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